

(3 hours)

Total Marks:80

N.B:

1. Question No .1 is compulsory.
2. Answer any **three** questions from **Q. 2 to Q. 6**
3. Use of statistical tables permitted.
4. Figures to the right indicate full marks.

- 1) (a) A continuous random variable x has the pdf $f(x) = kx^2e^{-x}$ where $x \geq 0$. Find k , its mean and variance. 5
- (b) State true or false with reasoning: $2x+y=3$ and $x=2y+3$ cannot be the lines of regression. 5
- (c) Find the relative maximum or minimum of the function $z=x_1^2+x_2^2+x_3^2-6x_1-8x_2-10x_3$. 5
- (d) Find the eigen values of $\text{adj.}A$ and A^2-2A+I where $A = \begin{bmatrix} 2 & 3 & 4 \\ 0 & 4 & 2 \\ 0 & 0 & 3 \end{bmatrix}$. 5
- 2) (a) Obtain the rank correlation coefficient from the following data. 6
- X: 10 12 18 18 15 40
- Y: 12 18 25 25 50 25
- (b) The marks obtained by the students in Maths ,Physics & Chemistry in an examination are normally distributed with the means 52,50 & 48 and with standard deviations 10 ,8 & 6 respectively. Find the probability that a student selected at random has secured a total of i) 180 or above ii) 135 or less. 6
- (c) Is the matrix $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$ diagonalisable? If so, find the diagonal form and the transformation matrix. 8
- 3) (a) If $A = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix}$, find A^{50} . 6
- (b) A die was thrown 132 times and the following frequencies were observed 6
- No: obtained : 1 2 3 4 5 6
- Frequencies : 15 20 25 15 29 28
- Test the hypothesis that the die is unbiased.
- (c) Use duality to solve the following linear programming problem. 8
- Minimise $Z = 4x_1+3x_2+6x_3$ subject to
- $x_1+x_3 \geq 2$;
- $x_2+x_3 \geq 5$, $x_1, x_2, x_3 \geq 0$.

4) (a) A sample of 100 students is taken from a large population. The mean height of the students in this sample is 160 cm. Can it be reasonably regarded that, in the population, the mean height is 165 cm and the SD is 10 cm?

(b) A transmission channel has a per digit error probability $p=0.01$. Calculate the probability of more than one error in 10 received digits using i) Binomial distribution ii) Poisson distribution.

(c) Evaluate $\int_0^{2\pi} \frac{1}{3+2\cos\theta} d\theta$.

5 .(a) Evaluate $\int \frac{1}{z^3(z+4)} dz$ where C is the circle $|z|=2$.

(b) show that the matrix $A = \begin{bmatrix} 5 & -6 & -6 \\ -1 & 4 & 2 \\ 3 & -6 & -4 \end{bmatrix}$ is derogatory.

(c) Samples of 2 types of electric bulbs were tested for length of life and the following data were obtained

	Size	Mean	SD
Sample 1	8	1234h	36h
Sample 2	7	1036h	40h

Is the difference in the means sufficient to warrant that type 1 bulbs are superior to type 2 bulbs?

6 (a). Using the Big-M penalty method, solve the following L.P.P

Minimise $Z=10x_1+3x_2$

subject to $x_1 + 2x_2 \geq 3$

$x_1 + 4x_2 \geq 4$ $x_1, x_2 \geq 0$.

(b) Use the Kuhn-Tucker conditions to solve the following N.L.P.P

Maximise $Z=2x_1^2 - 7x_2^2 + 12x_1x_2$

Subject to $2x_1 + 5x_2 \leq 98$ $x_1, x_2 \geq 0$

(c) Obtain Taylor's and Laurent's expansion for $f(z) = \frac{z-1}{(z-3)(z+1)}$ indicating the regions of convergence.

(Hours: 3 hrs)

[Total Marks: 80]

Note: 1. Question no. 1 is compulsory.2. Attempt any **three** questions out of remaining **five** questions.

- Q.1.[a]** Given two lines of regression lines $x + 2y - 5 = 0$, $2x + 3y + 8 = 0$. [5]
Find (i) $\bar{x}$, $\bar{y}$ (ii) correlation coefficient r .
- [b]** Show that $97 \mid (2^{48} - 1)$. [5]
- [c]** The probability density function of a random variable x is zero except at [5]
 $x = 0, 1, 2$ and $p(0) = 3k^3$, $p(1) = 4k - 10k^2$, $p(2) = 5k - 1$.
Find (i) k (ii) $p(0 < x \leq 2)$.
- [d]** Give an example of a graph which has [5]
(i) Eulerian circuit but not a Hamiltonian circuit
(ii) Hamiltonian circuit but not an Eulerian circuit
- Q.2.[a]** Find gcd (2947, 3997) using Euclidean Algorithm. Also find x and y [6]
such that $2947x + 3997y = \gcd(2947, 3997)$.
- [b]** The four roots of unity 1, -1, i , $-i$ forms a group under multiplication. [6]
- [c]** Find whether the following graphs $G = (V, E)$ and $G' = (V', E')$ are [8]
isomorphic? Justify.
(1) $V = \{a, b, c, d\}$, $E = \{(a, b), (a, d), (b, d), (c, d), (c, b), (c, d)\}$
(2) $V' = \{1, 2, 3, 4\}$, $E' = \{(1, 2), (2, 3), (3, 1), (3, 4), (4, 1), (4, 2)\}$
- Q.3.[a]** Show that $(D_8, \leq)$ is a lattice. Draw its Hasse diagram. [6]
- [b]** The local authorities in a certain city install 10,000 electric lamps in the [6]
streets of the city. If these lamps have an average life of 1000 burning
hours with a standard deviation of 200 hours, how many lamps might be
expected to fail i) in the first 800 burning hours?
ii) Between 800 and 1200 burning hours?
- [c]** (i) Find inverse of $2^{-1} \pmod{31}$ using Fermat's theorem. [8]
(ii) Find the Legendre's symbol of $\left(\frac{19}{23}\right)$.
- Q.4.[a]** Calculate the coefficient of correlation between x and y from the [6]
following data
- | | | | | | | | |
|-----|----|---|---|----|----|----|---|
| x | 12 | 9 | 8 | 10 | 11 | 13 | 7 |
| y | 14 | 8 | 6 | 9 | 11 | 12 | 3 |
- [b]** (i) Draw a connected graph for which every edge is a cut edge. [6]
(ii) Show that any connected graph with ' $n-1$ ' edges is a tree.

TURN OVER

- [c] (i) Can it be concluded that the average lifespan of an Indian is more than 70 years if a random sample of 100 Indians has an average lifespan of 71.8 years with standard deviation of 8.9 years? [8]
 (ii) Ten individuals are chosen at random from a population and their heights are found to be in inches 63, 63, 64, 65, 66, 69, 69, 70, 70, 71. Discuss the suggestion that the mean height of the universe is 65 inches.

Q.5.[a] Solve $x \equiv 5 \pmod{6}$, $x \equiv 4 \pmod{11}$, $x \equiv 3 \pmod{17}$. [6]

[b] Theory predicts that the proportion of beans in the four groups A, B, C, D should be 9:3:3:1. In an experiment among 1600 beans the numbers in the four groups were 882, 313, 287 and 118. Using Chi-Square verify does the experimental results support the theory? [6]

[c] Let G be a group of all permutations of degree 3 on 3 symbols 1, 2 & 3. Let $H = \{I, (1\ 2)\}$ be a subgroup of G. find all the distinct left cosets of H in G and hence index of H. [8]

Q.6.[a] Show that $53^{103} + 103^{53}$ is divisible by 39. [6]

[b] Given $L = \{1, 2, 4, 5, 10, 20\}$ with divisibility relation. Verify that $(L, \leq)$ is a distributive but not complemented Lattice. [6]

[c] (i) Write the following permutation as the product of disjoint cycles
 $f = (1\ 2)(1\ 2\ 3)(1\ 2)$. [8]

(ii) Express the expression $(x+y)(x+z)(x'y)'$ in the sum-of-product form.

22

15/12/18

Sem IV IT - CBCWS, Dec 18

Q. P. Code: 40017

Duration: 3 Hours

Marks: 80

N.B. (1) Question No. 1 is compulsory.

(2) Solve any three questions from remaining questions.

(3) Draw suitable diagrams wherever necessary.

(4) Assume suitable data, if necessary.

Q.1 Attempt any four sub-questions.

a) State and explain advantages and limitation of regular and context free grammar.

b) Design a Mealy machine for a binary adder.

c) Give formal definition of PDA.

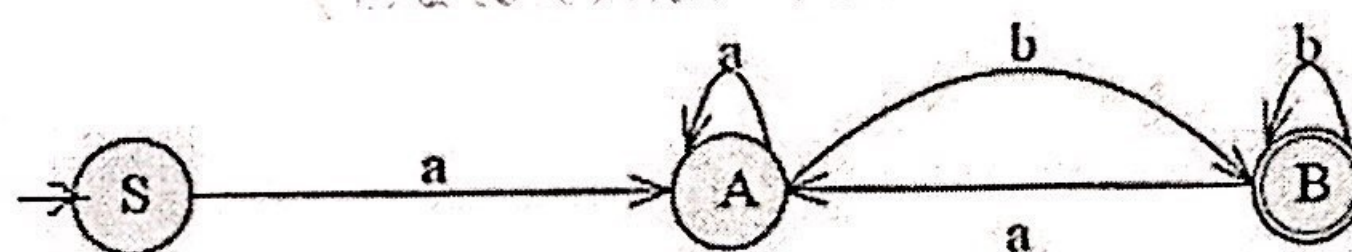
d) Construct the DFA that accept set of all strings over the alphabet $\Sigma = \{a, b\}$ containing either the substring 'aaa' or 'bbb'.

e) Find the CNF equivalent to

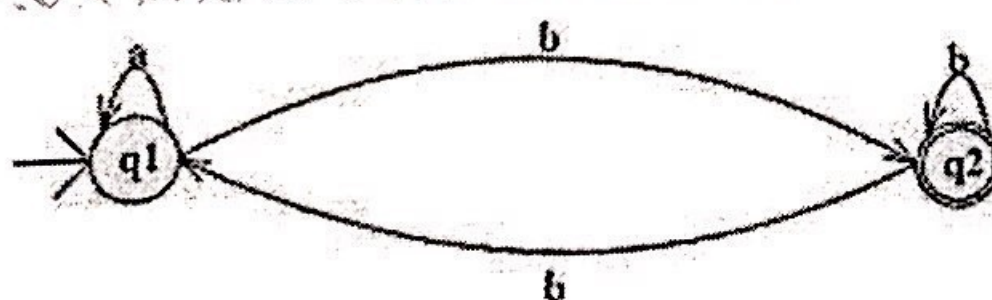
$S \rightarrow aAbB, A \rightarrow aA \mid a, B \rightarrow bB \mid b.$

Q2. a) What is NFA? Design a NFA for a binary number where the first and last digit is same.

b) Write a necessary function for the given automata.



Q3.a) i) Find a regular expression RE corresponding to the following FA



ii) Give a regular expression for a language over the alphabet $\Sigma = \{a, b\}$ containing at most two a's

b) Construct a Mealy machine that accepts strings ending in '00' and '11'. Convert the same to Moore machine.

Q4.a) Design a PDA for CFL that checks the well formedness of parenthesis i.e the language
 L of all balanced string of two types of paranthesis "(" and "[".
 Trace the sequence of moves made corresponding to input string (([])[]).

b) Construct a TM accepting palindromes over $\Sigma = \{a, b\}$.

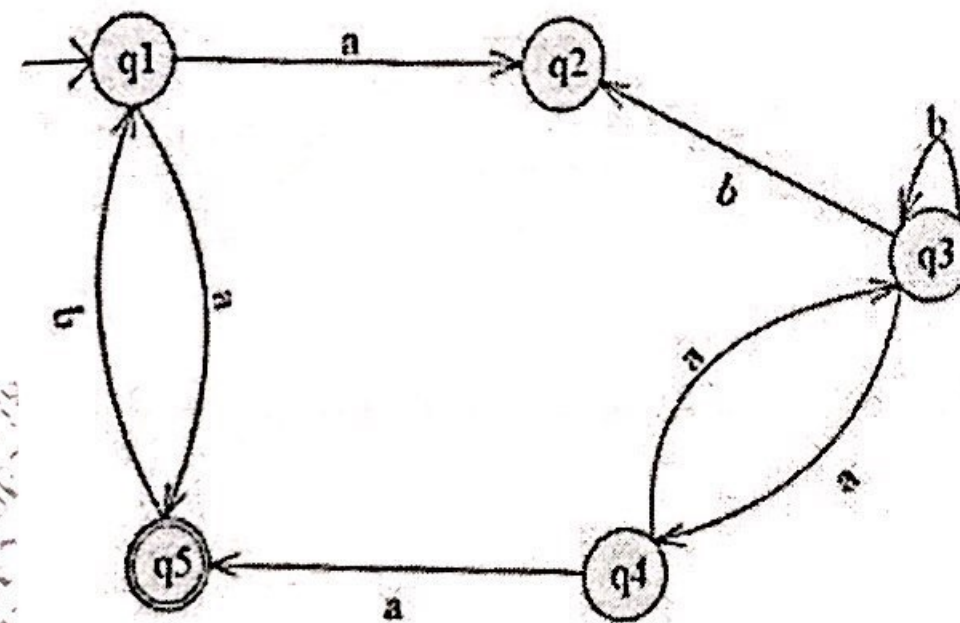
Q5. a) Let G be the grammar. Find the leftmost derivation, rightmost derivation and parse tree for the string 001222.

G: $S \rightarrow 0S \mid 1A \mid 2B \mid \epsilon$

$A \rightarrow 1A \mid 2B \mid \epsilon$

$B \rightarrow 2B \mid \epsilon$

b) Design a NFA for accepting input strings that contain either the keyword 000
 or the keyword 010 and convert it into an equivalent DFA.



Q6. Write short notes on (any four)

- Variants of Turing Machines
- Algorithm for CFG to CNF Conversion
- Chomsky Hierarchy
- Limitation of Finite Automata
- Halting Problem.

Duration: 3 hours

Total marks: 80

Note (1) Question No. 1 is compulsory

(2) Attempt any three questions from remaining questions

(3) Draw suitable diagrams wherever necessary

(4) Assume suitable data, if necessary

Q 1. (a) Find the CFG for the regular expression $(10)^*(110+01)^*$. (05)

(b) Write short note on Universal Turing Machine. (05)

(c) Difference between FA and PDA (05)

(d) Design moore machine to convert each occurrence of 111 to 101 (05)

Q 2. (a) Construct NFA with epsilon which accept a language consisting the string of any number of a's followed by any number of b's followed by any number of c's. (10)

Also convert it into NFA without epsilon.

(b) Design a Moore and Mealy machine for a binary input sequence such that if it has a substring 011 the machine outputs A if input has substring 001 it outputs B otherwise it outputs C. (10)

Q 3 (a) Minimize the following DFA where A is a start state and B, C and E are final states. (10)

∂	0	1
A	D	B
B	C	F
C	C	F
D	A	E
E	C	F
F	F	F

Q.P. Code: 25528

(b) Use pumping lemma prove that whether following language is regular or not (10)

$$(a^n b^n c^n \mid n \geq 1)$$

Q 4 (a) Define context free grammar. Obtain the CFG for the following regular expression: (10)

$$(110 + 11)^* (10)^*$$

(b) Convert given CFG to GNF where $V = \{S, A\}$, $T = \{0, 1\}$ and P is (10)

$$S \rightarrow AA \mid 0$$

$$A \rightarrow SS \mid 1$$

Q 5 (a) Design a PDA to accept a string of balanced parentheses. The parentheses (10)

to be considered (,) , { , }.

(b) Construct TM for $L = \{a^n b^n c^n \mid n \geq 1\}$ (10)

Q 6 Write short notes on (Any two) (20)

(a) Pumping Lemma for Regular Languages

(b) Recursive and Recursively enumerable languages

(c) Unsolvable Problems

[Time: Three Hours]

[Marks:80]

Note:

- 1) Question 1 is compulsory.
- 2) Solve any three questions out of the remaining questions

Q1

- (a) Discuss and compare various types of networks. **05**
- (b) The size option field of an IP datagram is 20 bytes. What is the value of HLEN? What is the value in binary? **05**
- (c) Compare connectionless and connection-oriented services. **05**
- (d) The received string of bits is 110011001100. Is it acceptable? If so, what is the data bit sequence? Consider the divisor is 10101. **05**

Q2 (a) What is routing in a network? Explain the shortest path routing protocol. **10**

Q2 (b) Explain the different transmission media in networking. **10**

Q3 (a) Explain OSI reference model and the services and functions of each layer. **10**

Q3 (b) Construct Huffman code for the given symbols $\{x_1, x_2, \dots, x_8\}$ with probabilities $P(x) = \{0.07, 0.08, 0.04, 0.26, 0.14, 0.09, 0.07, 0.25\}$. Find the coding efficiency. **10**

Q4 (a) Explain TCP segment header format in detail. **10**

Q4 (b) Explain ALOHA and Slotted ALOHA. **10**

Q5 (a) What is congestion and what are the causes of congestion? Explain token bucket algorithm of congestion control. **10**

Q5 (b) Explain CSMA/CD. **10**

Q6 Write short notes on the following (any four): **20**

- a. SMTP
- b. HDLC
- c. ARP, RARP
- d. Traditional Ethernet frame
- e. Hubs, switches, bridges

Q.P. Code : 13122

[Time: Three Hours]

[Marks:80]

Please check whether you have got the right question paper.

N.B: 1. Question No 1 is compulsory.

2. Attempt any three questions out of remaining questions.

- Q. 1** Answer **any four** from the following. **20**
- "Internet has a connectionless service at network layer." Is the statement true or false? Justify your answer.
 - Define framing and state reason for its need.
 - Differentiate between slotted ALOHA and Pure ALOHA.
 - Explain Go - Back - N ARQ.
 - Differentiate between a physical address and a logical address.
- Q. 2**
 - What is OSI model? Give function and services of each layer. **10**
 - Explain the different Guided transmission media in networking. **10**
- Q. 3**
 - In an IPv4 packet, the value of HLEN is 1000 in binary. How many bytes of options are being carried by this packet? **04**
 - Explain IP address and subnet mask. **06**
 - Differentiate between UDP and TCP. **10**
- Q. 4**
 - Explain Sliding Window protocol with neat diagram. **10**
 - Explain CRC with example. **10**
- Q. 5**
 - What is routing? Explain different categories of routing algorithms. **10**
 - Draw and Explain TCP segment header. **10**
- Q. 6** Write short notes on the following (**any four**): **20**
- Networking using Windows and LINUX operating system
 - Mobile Telephone system
 - Hub, Switches, Router
 - Network topology
 - Communication satellite

(3 Hours)

[Total Marks: 80]

Note : Q1 is compulsory.

Attempt any THREE out of the remaining questions.

Assume suitable data if necessary.

Q1. Attempt any 4 sub questions

- | | |
|--|----|
| a) Explain six stage instruction pipeline with suitable diagram. | 5 |
| b) Write a note on 8288 bus controller. | 5 |
| c) Explain memory hierarchy. | 5 |
| d) Draw the flowchart of unsigned binary restoring division algorithm. | 5 |
| e) Explain any five instructions of 8086 microprocessor with suitable examples. | 5 |
| | |
| Q2. a) What is DMA? Explain working of DMA. | 10 |
| b) List and explain key characteristics of computer memory. | 10 |
| | |
| Q3. a) Draw the flowchart of Booths algorithm and multiply $(-3) \times (4)$ using Booths algorithm. | 10 |
| b) Explain micro-programmed control unit with suitable diagram. | 10 |
| | |
| 4. a) Explain addressing modes of 8086 microprocessor with suitable examples. | 10 |
| b) Explain single and double precision IEEE 754 binary floating point representation formats. | 10 |
| | |
| Q5. a) Explain with suitable diagram maximum mode of operation of 8086 Micro processor. | 10 |
| b) Write 8086 Assembly Language Program to count number of 0's and 1's in a given 8 bit number. | 10 |
| | |
| Q6. Write notes on (any two) | 20 |
| a) Cache memory mapping techniques. | |
| b) Flynn's classification of parallel computers. | |
| c) Programmed I/O. | |

(3 Hours)

[Total Marks: 80]

Note : Q1 is compulsory.

Attempt any THREE out of the remaining questions.

Assume suitable data if necessary.

Q1. Attempt any 4 sub questions

- a) Differentiate between computer architecture and organization. (5 M)
- b) What is instruction pipelining? Explain. (5 M)
- c) Draw the flowchart of unsigned binary restoring division algorithm. (5 M)
- d) What is a micro-program? Give suitable example. (5 M)
- e) Explain computer memory hierarchy. (5 M)

- Q2. a) What is stored program concept? Explain Von-Neumann architecture. (10 M)
- b) Differentiate between hardwired and microprogrammed approach. (10 M)

- Q3 a) Represent the number $(-0.0625)_{10}$ in single and double precision IEEE 754 binary floating point representation formats. (10 M)
- b) What are Pipeline Hazards? Explain different types of Pipeline Hazards. (10 M)

- 4 a) Explain addressing modes with suitable examples. (10 M)
- b) Draw the flowchart of Booths algorithm and multiply $(-7) \times (3)$ using Booths algorithm. (10 M)

- Q5. a) Explain Interrupt driven I/O. (10 M)
- b) Explain different cache memory mapping techniques. (10 M)

- Q6 Write notes on (any two) (20 M)
- a) Interleaved and Associative memory.
 - b) DMA.
 - c) Instruction execution cycle with interrupt processing.

NOTE: Question No 1 is compulsory. Attempt any three questions from remaining.

Assume suitable data if necessary.

Draw neat labelled diagrams wherever needed.

- Q.1. a) Explain the two main categories of services and functions of operating system. **10M**
Compare and contrast them.
- b) What is context-switch? Describe the actions taken by a kernel to context-switch between processes. **10M**
- Q.2. a) Explain the differences in how much the following scheduling algorithms discriminate in favor of short processes: **10M**
a. FCFS
b. RR
c. Multilevel feedback queues
- b) Describe the differences among short-term, medium-term, and long-term scheduling. **10M**
- Q.3. a) Explain the timestamp based protocols to ensure serializability with the help of example. **10M**
- b) Consider the following set of processes, with the length of the CPU burst given in milli seconds. The processes are assumed to have arrived in order P₁, P₂, P₃, P₄, P₅ all at time 0. **10M**

Process	Burst Time	Priority
P ₁	10	3
P ₂	1	1
P ₃	2	3
P ₄	1	4
P ₅	5	2

Calculate the average turnaround time and maximum waiting time for pre-emptive priority scheduling algorithm.

- Q.4. a) Compare and contrast paging and segmentation. **10M**
- b) What is address translation? Consider a logical address space of 32 pages with 1,024 words per page, mapped onto a physical memory of 16 frames. **10M**
a. How many bits are required in the logical address?
b. How many bits are required in the physical address?
- Q.5. a) Describe how the Swap () instruction can be used to provide mutual exclusion that satisfies the bounded-waiting requirement. **10M**
- b) What is deadlock? What are the essential conditions for deadlock to occur? **10M**
- Q.6. Write Short Notes on: **(Any four)** **20M**
a) Linked Allocation.
b) Memory segmentation
c) Deadlock detection.
d) Translation Lookaside Buffer
e) Open() and Close () operations.
f) Page replacement algorithms
